

## SOME PROPERTIES OF $(1, 2)^*$ - $\check{g}_\alpha$ -LOCALLY CLOSED SETS

<sup>1,2</sup>K. BALASUBRAMANIYAN AND <sup>3</sup>K. SRIDHARAN

<sup>1</sup>Department of Mathematics,  
Annamalai University, Annamalainagar-608 002, Chidambaram, Tamil Nadu, India.

Deputed: <sup>2</sup>Department of Mathematics, Arignar Anna Government Arts College,  
Vadachennimalai-636 121, Salem District, Tamil Nadu, India.

e-mail : <sup>1,2</sup>kgbalumaths@gmail.com

<sup>3</sup>Department of Information Technology, Panimalar Engineering College,  
Chennai, Tamil Nadu, India.

e-mail : <sup>3</sup>drsridharank.p@gmail.com

ABSTRACT. In present of this paper, we introduce a new classes of sets namely  $(1, 2)^*$ - $\Lambda_G$ -sets,  $(1, 2)^*$ - $\lambda_G$ -sets and  $(1, 2)^*$ - $\check{g}_\alpha$ -Locally closed sets are study in bitopological spaces. Also discuss some essential properties of  $(1, 2)^*$ - $\check{g}_\alpha$ -closed sets.

### 1. INTRODUCTION

In the perceptions of bitopological spaces was introduced and studied by J. C. Kelly [3] . Recently, More generalizations of closed sets and it is properties were introduced and investigated by various researchers for some example ([7, 6, 10]) and so on.

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Corresponding Author: \*K.Balasubramaniyan.

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In present of this paper, we introduce a new classes of sets namely  $(1, 2)^*$ - $\Lambda_G$ -sets,  $(1, 2)^*$ - $\lambda_G$ -sets and  $(1, 2)^*$ - $\check{g}_\alpha$ -Locally closed sets are study in bitopological spaces. Also discuss some essential properties of  $(1, 2)^*$ - $\check{g}_\alpha$ -closed sets.

## 2. PRELIMINARIES

Throughout this paper  $(X, \tau_1, \tau_2)$  and  $(Y, \sigma_1, \sigma_2)$  (or simply  $X$  and  $Y$ ) represents the non-empty bitopological spaces on which no separation axiom are assumed, unless otherwise mentioned. For a subset  $A$  of  $X$ ,  $\tau_{1,2}\text{-cl}(A)$  and  $\tau_{1,2}\text{-int}(A)$  represents the closure of  $A$  and interior of  $A$  respectively.

**Definition 2.1.** [4] *A subset  $A$  of a bitopological space  $(X, \tau_1, \tau_2)$  or  $X$  is called*

- (1) *a  $(1, 2)^*$ -semi open set if  $A \subseteq \tau_{1,2}\text{-cl}(\tau_{1,2}\text{-int}(A))$ .*
- (2) *a  $(1, 2)^*$ -pre open set if  $A \subseteq \tau_{1,2}\text{-int}(\tau_{1,2}\text{-cl}(A))$ .*
- (3) *a  $(1, 2)^*$ - $\alpha$ -open set if  $A \subseteq \tau_{1,2}\text{-int}(\tau_{1,2}\text{-cl}(\tau_{1,2}\text{-int}(A)))$ .*
- (4) *a  $(1, 2)^*$ - $\beta$ -open (or) a  $(1, 2)^*$ -semi-pre open set [9] if  $A \subseteq \tau_{1,2}\text{-cl}(\tau_{1,2}\text{-int}(\tau_{1,2}\text{-cl}(A)))$ .*

The complements of the above mentioned sets are called their respective closed sets.

**Definition 2.2.** *A subset  $A$  of a bitopological space  $(X, \tau_1, \tau_2)$  or  $X$  is said to be*

- (1) *a  $(1, 2)^*$ -generalized closed set (briefly,  $(1, 2)^*$ -g-closed) [10] if  $\tau_{1,2}\text{-cl}(A) \subseteq U$  whenever  $A \subseteq U$  and  $U$  is  $\tau_{1,2}$ -open.*
- (2) *a  $(1, 2)^*$ -semi generalized closed set (briefly,  $(1, 2)^*$ -sg-closed) [8] if  $(1, 2)^*\text{-scl}(A) \subseteq U$  whenever  $A \subseteq U$  and  $U$  is  $(1, 2)^*$ -semi-open.*
- (3) *a  $(1, 2)^*$ -generalized semi-closed (briefly,  $(1, 2)^*$ -gs-closed) set [1] if  $(1, 2)^*\text{-scl}(A) \subseteq U$  whenever  $A \subseteq U$  and  $U$  is  $\tau_{1,2}$ -open.*

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- (4) an  $(1, 2)^*$ - $\alpha$ -generalized closed (briefly,  $(1, 2)^*$ - $\alpha$ g-closed) set [5] if  $(1, 2)^*$ - $\alpha$ cl( $A$ )  $\subseteq U$  whenever  $A \subseteq U$  and  $U$  is  $\tau_{1,2}$ -open.
- (5) a  $(1, 2)^*$ -generalized semi-preclosed (briefly,  $(1, 2)^*$ -gsp-closed) set [5] if  $(1, 2)^*$ - $\beta$ cl( $A$ )  $\subseteq U$  whenever  $A \subseteq U$  and  $U$  is  $\tau_{1,2}$ -open.
- (6) a  $(1, 2)^*$ - $\hat{g}$ -closed set [7] if  $\tau_{1,2}$ -cl( $A$ )  $\subseteq U$  whenever  $A \subseteq U$  and  $U$  is  $(1, 2)^*$ -sg-open.
- (7) a  $(1, 2)^*$ - $\hat{g}_1$ -closed set [6] if  $\tau_{1,2}$ -cl( $A$ )  $\subseteq U$  whenever  $A \subseteq U$  and  $U$  is  $(1, 2)^*$ - $\hat{g}$ -open.
- (8) a  $(1, 2)^*$ - $\mathcal{G}$ -closed set [6] if  $(1, 2)^*$ -scl( $A$ )  $\subseteq U$  whenever  $A \subseteq U$  and  $U$  is  $(1, 2)^*$ - $\hat{g}_1$ -open.
- (9) a  $(1, 2)^*$ - $\check{g}$ -closed set [6] if  $\tau_{1,2}$ -cl( $A$ )  $\subseteq U$  whenever  $A \subseteq U$  and  $U$  is  $(1, 2)^*$ - $\mathcal{G}$ -open.
- (10) a  $(1, 2)^*$ - $\check{g}_\alpha$ -closed set [2] if  $\tau_{1,2}$ - $\alpha$ cl( $A$ )  $\subseteq U$  whenever  $A \subseteq U$  and  $U$  is  $(1, 2)^*$ - $\mathcal{G}$ -open.

The complements of the above mentioned closed sets are called their respective open sets.

**Proposition 2.3.** [2] In a space  $(X, \tau_1, \tau_2)$ , every  $(1, 2)^*$ - $\alpha$ -closed set is  $(1, 2)^*$ - $\check{g}_\alpha$ -closed.

3. PROPERTIES OF  $(1, 2)^*$ - $\check{g}_\alpha$ -CLOSED SETS

**Definition 3.1.** The intersection of all  $(1, 2)^*$ - $\mathcal{G}$ -open subsets in  $(X, \tau_1, \tau_2)$  containing  $A$  is said to be a  $(1, 2)^*$ - $\mathcal{G}$ -kernel of  $A$  and denoted by  $(1, 2)^*$ - $\mathcal{G}$ -ker( $A$ ).

**Lemma 3.2.** A subset  $A$  of  $(X, \tau_1, \tau_2)$  is  $(1, 2)^*$ - $\check{g}_\alpha$ -closed  $\iff \tau_{1,2}$ - $\alpha$ cl( $A$ )  $\subseteq (1, 2)^*$ - $\mathcal{G}$ -ker( $A$ ).

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*Proof.* Suppose that  $A$  is  $(1, 2)^*$ - $\check{g}_\alpha$ -closed. Then  $(1, 2)^*$ - $\alpha cl(A) \subseteq U$  whenever  $A \subseteq U$  and  $U$  is  $(1, 2)^*$ - $\mathcal{G}$ -open. Let  $x \notin \tau_{1,2}\text{-}\alpha cl(A)$ . If  $x \notin (1, 2)^*$ - $\mathcal{G}\text{-ker}(A)$ , then there is  $(1, 2)^*$ - $\mathcal{G}$ -open set  $U$  containing  $A$  such that  $x \notin U$ . Since  $U$  is  $(1, 2)^*$ - $\mathcal{G}$ -open set containing  $A$ , we have  $x \notin \tau_{1,2}\text{-}\alpha cl(A)$  and this is a contradiction.

Conversely, let  $\tau_{1,2}\text{-}\alpha cl(A) \subseteq (1, 2)^*$ - $\mathcal{G}\text{-ker}(A)$ . If  $U$  is any  $(1, 2)^*$ - $\mathcal{G}$ -open set containing  $A$ , then  $\tau_{1,2}\text{-}\alpha cl(A) \subseteq (1, 2)^*$ - $\mathcal{G}\text{-ker}(A) \subseteq U$ . Therefore,  $A$  is  $(1, 2)^*$ - $\check{g}_\alpha$ -closed.

**Theorem 3.3.** *If  $A$  and  $B$  are  $(1, 2)^*$ - $\check{g}_\alpha$ -closed sets in  $(X, \tau_1, \tau_2)$ , then  $A \cup B$  is  $(1, 2)^*$ - $\check{g}_\alpha$ -closed in  $(X, \tau_1, \tau_2)$ .*

*Proof.* If  $A \cup B \subseteq U$  and  $U$  is  $(1, 2)^*$ - $\mathcal{G}$ -open, then  $A \subseteq U$  and  $B \subseteq U$ . Since  $A$  and  $B$  are  $(1, 2)^*$ - $\check{g}_\alpha$ -closed,  $U \supseteq \tau_{1,2}\text{-}\alpha cl(A)$  and  $U \supseteq \tau_{1,2}\text{-}\alpha cl(B)$  and hence  $U \supseteq \tau_{1,2}\text{-}\alpha cl(A) \cup \tau_{1,2}\text{-}\alpha cl(B) = \tau_{1,2}\text{-}\alpha cl(A \cup B)$ . Thus  $A \cup B$  is  $(1, 2)^*$ - $\check{g}_\alpha$ -closed in  $(X, \tau_1, \tau_2)$ .

**Theorem 3.4.** *If a set  $A$  is  $(1, 2)^*$ - $\check{g}_\alpha$ -closed in  $(X, \tau_1, \tau_2)$  and  $A \subseteq B \subseteq \tau_{1,2}\text{-}\alpha cl(A)$ , then  $B$  is  $(1, 2)^*$ - $\check{g}_\alpha$ -closed in  $(X, \tau_1, \tau_2)$ .*

*Proof.* Let  $U$  be  $(1, 2)^*$ - $\mathcal{G}$ -open set in  $(X, \tau_1, \tau_2)$  such that  $B \subseteq U$ . Then  $A \subseteq U$ . Since  $A$  is an  $(1, 2)^*$ - $\check{g}_\alpha$ -closed set,  $\tau_{1,2}\text{-}\alpha cl(A) \subseteq U$ . Also  $\tau_{1,2}\text{-}\alpha cl(B) = \tau_{1,2}\text{-}\alpha cl(A) \subseteq U$ . Hence  $B$  is also an  $(1, 2)^*$ - $\check{g}_\alpha$ -closed in  $(X, \tau_1, \tau_2)$ .

**Theorem 3.5.** *If  $A$  is  $(1, 2)^*$ - $\mathcal{G}$ -open and  $(1, 2)^*$ - $\check{g}_\alpha$ -closed in  $(X, \tau_1, \tau_2)$ , then  $A$  is  $(1, 2)^*$ - $\alpha$ -closed in  $(X, \tau_1, \tau_2)$ .*

*Proof.* Since  $A$  is  $(1, 2)^*$ - $\mathcal{G}$ -open and  $(1, 2)^*$ - $\check{g}_\alpha$ -closed,  $\tau_{1,2}\text{-}\alpha cl(A) \subseteq A$  and hence  $A$  is  $(1, 2)^*$ - $\alpha$ -closed in  $(X, \tau_1, \tau_2)$ .

**Theorem 3.6.** *For each  $x \in X$ , either  $\{x\}$  is  $(1, 2)^*$ - $\mathcal{G}$ -closed or  $\{x\}^c$  is  $(1, 2)^*$ - $\check{g}_\alpha$ -closed in  $(X, \tau_1, \tau_2)$ .*

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*Proof.* Suppose that  $\{x\}$  is not  $(1, 2)^*$ - $\mathcal{G}$ -closed in  $(X, \tau_1, \tau_2)$ . Then  $\{x\}^c$  is not  $(1, 2)^*$ - $\mathcal{G}$ -open and the only  $(1, 2)^*$ - $\mathcal{G}$ -open set containing  $\{x\}^c$  is the space  $X$  itself. Therefore  $\tau_{1,2}\text{-}\alpha\text{cl}(\{x\}^c) \subseteq X$  and so  $\{x\}^c$  is  $(1, 2)^*$ - $\mathcal{G}$ -closed in  $(X, \tau_1, \tau_2)$ .

**Definition 3.7.** A subset  $A$  of a space  $(X, \tau_1, \tau_2)$  is said to be  $(1, 2)^*$ - $\Lambda_{\mathcal{G}}$ -set if  $A = (1, 2)^*$ - $\mathcal{G}$ -ker( $A$ ).

**Definition 3.8.** A subset  $A$  of a space  $(X, \tau_1, \tau_2)$  is called  $(1, 2)^*$ - $\lambda_{\mathcal{G}}$ -closed if  $A = S \cap T$  where  $S$  is a  $(1, 2)^*$ - $\Lambda_{\mathcal{G}}$ -set and  $T$  is  $(1, 2)^*$ - $\alpha$ -closed.

The complement of  $(1, 2)^*$ - $\lambda_{\mathcal{G}}$ -closed set is called  $(1, 2)^*$ - $\lambda_{\mathcal{G}}$ -open set.

The collection of all  $(1, 2)^*$ - $\lambda_{\mathcal{G}}$ -closed (resp.  $(1, 2)^*$ - $\lambda_{\mathcal{G}}$ -open) sets in  $(X, \tau_1, \tau_2)$  is denoted by  $(1, 2)^*$ - $\lambda_{\mathcal{G}}C(X)$  (resp.  $(1, 2)^*$ - $\lambda_{\mathcal{G}}O(X)$ ).

**Lemma 3.9.** For a subset  $A$  of a topological space  $(X, \tau_1, \tau_2)$ , the following conditions are equivalent.

- (1)  $A$  is  $(1, 2)^*$ - $\lambda_{\mathcal{G}}$ -closed.
- (2)  $A = S \cap \tau_{1,2}\text{-}\alpha\text{cl}(A)$  where  $S$  is a  $(1, 2)^*$ - $\Lambda_{\mathcal{G}}$ -set.
- (3)  $A = (1, 2)^*$ - $\mathcal{G}$ -ker( $A$ )  $\cap$   $\tau_{1,2}\text{-}\alpha\text{cl}(A)$ .

**Lemma 3.10.** In a space  $(X, \tau_1, \tau_2)$ ,

- (1) every  $(1, 2)^*$ - $\alpha$ -closed set is  $(1, 2)^*$ - $\lambda_{\mathcal{G}}$ -closed.
- (2) every  $(1, 2)^*$ - $\Lambda_{\mathcal{G}}$ -set is  $(1, 2)^*$ - $\lambda_{\mathcal{G}}$ -closed.

**Remark 3.11.** The converses of Lemma 3.10 need not be true as seen from the following Examples.

**Example 3.12.** Let  $X = \{a, b, c, d, e\}$  with  $\tau_1 = \{\phi, \{a\}, X\}$  and  $\tau_2 = \{\phi, X\}$  then  $\tau_{1,2} = \{\phi, \{a\}, X\}$ , we have

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- (1)  $(1, 2)^*-\alpha C(X) = \{\phi, \{b\}, \{c\}, \{b, c\}, X\}$  and  $(1, 2)^*-\lambda_{\mathcal{G}}C(X) = \wp(X)$ . In the space  $X$ , then the subset  $\{a\}$  is  $(1, 2)^*-\lambda_{\mathcal{G}}$ -closed set but not  $(1, 2)^*-\alpha$ -closed.
- (2)  $(1, 2)^*-\Lambda_{\mathcal{G}}$ -sets are  $\{\phi, \{a\}, \{a, b\}, \{a, c\}, X\}$  and  $(1, 2)^*-\lambda_{\mathcal{G}}C(X) = \wp(X)$ . In the space  $X$ , then the subset  $\{b\}$  is  $(1, 2)^*-\lambda_{\mathcal{G}}$ -closed set but not  $(1, 2)^*-\Lambda_{\mathcal{G}}$ -set.

**Theorem 3.13.** For a subset  $A$  of a topological space  $(X, \tau_1, \tau_2)$ , the following conditions are equivalent.

- (1)  $A$  is  $(1, 2)^*-\alpha$ -closed.
- (2)  $A$  is  $(1, 2)^*-\check{g}_{\alpha}$  and  $(1, 2)^*-\lambda_{\mathcal{G}}$ .

*Proof.* (1)  $\Rightarrow$  (2). Obvious.

(2)  $\Rightarrow$  (1). Since  $A$  is  $(1, 2)^*-\check{g}_{\alpha}$ -closed, so by Lemma 3.2,  $\tau_{1,2}-\alpha cl(A) \subseteq (1, 2)^*-\mathcal{G}-ker(A)$ . Since  $A$  is  $(1, 2)^*-\lambda_{\mathcal{G}}$ -closed, so by Lemma 3.9,  $A = (1, 2)^*-\mathcal{G}-ker(A) \cap \tau_{1,2}-cl(A) = \tau_{1,2}-cl(A)$ . Hence  $A$  is  $(1, 2)^*-\alpha$ -closed.

**Remark 3.14.** The following examples show that concepts of  $(1, 2)^*-\check{g}_{\alpha}$ -closed sets and  $(1, 2)^*-\lambda_{\mathcal{G}}$ -closed sets are independent of each other.

**Example 3.15.** In Example 3.12, we have  $(1, 2)^*-\check{g}_{\alpha}C(X) = \{\phi, \{b\}, \{c\}, \{b, c\}, X\}$  and  $(1, 2)^*-\lambda_{\mathcal{G}}C(X) = \wp(X)$ . In the space  $X$ , then the subset  $\{a\}$  is  $(1, 2)^*-\lambda_{\mathcal{G}}$ -closed set but not  $(1, 2)^*-\check{g}_{\alpha}$ -closed.

**Example 3.16.** Let  $X = \{a, b, c\}$  with  $\tau_1 = \{\phi, \{a, b\}, X\}$  and  $\tau_2 = \{\phi, X\}$  then  $\tau_{1,2} = \{\phi, \{a, b\}, X\}$ . We have  $(1, 2)^*-\check{g}_{\alpha}C(X) = \{\phi, \{c\}, \{a, c\}, \{b, c\}, X\}$  and  $(1, 2)^*-\lambda_{\mathcal{G}}C(X) = \{\phi, \{a\}, \{b\}, \{c\}, \{a, b\}, X\}$ . In the space  $X$ , then the subset  $\{a\}$  is  $(1, 2)^*-\lambda_{\mathcal{G}}$ -closed set but not  $(1, 2)^*-\check{g}_{\alpha}$ -closed.

SOME PROPERTIES OF  $(1, 2)^*$ - $\check{g}_\alpha$ -LOCALLY CLOSED SETS4. ON  $(1, 2)^*$ - $\check{g}_\alpha$ -LOCALLY CLOSED SETS

**Definition 4.1.** Let  $(X, \tau_1, \tau_2)$  be a bitopological space. A subset  $A$  of  $X$  is called  $(1, 2)^*$ - $\check{g}_\alpha$ -Locally closed sets (briefly  $(1, 2)^*$ - $\check{g}_\alpha$ -Lc) if  $A = S \cap T$  where  $S$  is  $(1, 2)^*$ - $\mathcal{G}$ -open and  $T$  is  $(1, 2)^*$ - $\alpha$ -closed in  $(X, \tau_1, \tau_2)$ .

**Example 4.2.** In Example 3.16, we have the subset  $\{a\}$  is  $(1, 2)^*$ - $\check{g}_\alpha$ -Lc-set in  $X$ .

**Proposition 4.3.** In a space  $(X, \tau_1, \tau_2)$ , every  $(1, 2)^*$ - $\mathcal{G}$ -open set is  $(1, 2)^*$ - $\check{g}_\alpha$ -Lc-set.

**Remark 4.4.** The converse of Proposition 4.3 need not be true seen from the following Example.

**Example 4.5.** In Example 3.16, we have  $(1, 2)^*$ - $\check{g}_\alpha$ -Lc-sets are  $\{\phi, \{a\}, \{b\}, \{c\}, \{a, b\}, X\}$  and  $(1, 2)^*$ - $\mathcal{G}$ -open sets are  $\{\phi, \{a\}, \{b\}, \{a, b\}, X\}$ . In the space  $X$ , then the subset  $\{c\}$  is  $(1, 2)^*$ - $\check{g}_\alpha$ -Lc-set but not  $(1, 2)^*$ - $\mathcal{G}$ -open.

**Proposition 4.6.** In a space  $(X, \tau_1, \tau_2)$ , every  $(1, 2)^*$ - $\alpha$ -closed set is  $(1, 2)^*$ - $\check{g}_\alpha$ -Lc-set.

**Remark 4.7.** The converse of Proposition 4.6 need not be true seen from the following Example.

**Example 4.8.** In Example 3.16, we have  $(1, 2)^*$ - $\check{g}_\alpha$ -Lc-sets are  $\{\phi, \{a\}, \{b\}, \{c\}, \{a, b\}, X\}$  and  $(1, 2)^*$ - $\alpha C(X) = \{\phi, \{c\}, X\}$ . In the space  $X$ , then the subset  $\{a\}$  is  $(1, 2)^*$ - $\check{g}_\alpha$ -Lc-set but not  $(1, 2)^*$ - $\alpha$ -closed.

**Theorem 4.9.** Let  $(X, \tau_1, \tau_2)$  be a bitopological space and  $A$  a subset of  $X$ . Then,  $A$  is  $(1, 2)^*$ - $\alpha$ -closed  $\iff$   $(1, 2)^*$ - $\check{g}_\alpha$ -closed and  $(1, 2)^*$ - $\check{g}_\alpha$ -Lc-set.

*Proof.* Let  $A$  be an  $(1, 2)^*$ - $\alpha$ -closed. By Propositions 2.3 and 4.6,  $A$  is  $(1, 2)^*$ - $\check{g}_\alpha$ -closed and  $(1, 2)^*$ - $\check{g}_\alpha$ -Lc-set.

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Conversely, let  $A = S \cap T$ . Then  $S$  is  $(1, 2)^*\mathcal{G}$ -open and  $T$  is  $(1, 2)^*\alpha$ -closed. Since  $A$  is  $(1, 2)^*\check{g}_\alpha$ -closed,  $\tau_{1,2}\text{-cl}(A) \subseteq S$ . Also  $\tau_{1,2}\text{-cl}(A) \subseteq \tau_{1,2}\text{-cl}(T) = T$ . We have  $\tau_{1,2}\text{-cl}(A) \subseteq S \cap T = A$ . Hence  $A$  is  $(1, 2)\text{-}\alpha$ -closed.

**Remark 4.10.** *The following Example shows that the concepts of  $(1, 2)^*\check{g}_\alpha$ -closed sets and  $(1, 2)^*\check{g}_\alpha$ -Lc-sets are independent of each other.*

**Example 4.11.** *In Example 3.16, we have  $(1, 2)^*\check{g}_\alpha$ -Lc- sets are  $\{\phi, \{a\}, \{b\}, \{c\}, \{a, b\}, X\}$  and  $(1, 2)^*\check{g}_\alpha C(X) = \{\phi, \{c\}, \{a, c\}, \{b, c\}, X\}$ . In the space  $X$ , then*

- (1) *the subset  $\{a\}$  is  $(1, 2)^*\check{g}_\alpha$ -Lc-set but not  $(1, 2)^*\check{g}_\alpha$ -closed.*
- (2) *the subset  $\{a, c\}$  is  $(1, 2)^*\check{g}_\alpha$ -closed set but not  $(1, 2)^*\check{g}_\alpha$ -Lc -set.*

## CONCLUSION

The notions of sets and functions in bitopological spaces and fuzzy topological spaces are extensively developed and used in many engineering problems, information systems, particle physics, computational topology and mathematical sciences.

By researching generalizations of closed sets, some new separation axioms have been founded and they turn out to be useful in the study of digital topology. Therefore, all bitopological sets and functions defined will have many possibilities of applications in digital topology and computer graphics.

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